

# $\eta$ and $\eta'$ Physics at BES-III

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## Abstract

Decays of both  $\eta$  and  $\eta'$  provide very useful information in our understanding of low-energy QCD, and experimental signatures for these decays would be extremely helpful at BES-III. The rare decays of the  $\eta$  and  $\eta'$  mesons could serve as a low-energy test of the Standard Model and its beyond. The sensitivities of the measurements of  $\eta$  and  $\eta'$  decays are discussed at BES-III, in which the  $\eta$  and  $\eta'$  mesons are produced in the  $\psi$  decays.

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## INTRODUCTION

Quantum chromodynamics (QCD), which is a field theory of strong interaction, cannot be directly applied in the low energy since the strong coupling  $\alpha_s$  is large [1, 2]. In this case one must resort to alternative model-independent approaches, such as lattice QCD, chiral perturbation theory (ChPT). The  $\eta$  and  $\eta'$  mesons play an important role in understanding the low energy QCD. They are isoscalar members of the nonet of the lightest pseudoscalar mesons. Decays of  $\eta$  and  $\eta'$  are investigated within a  $U(3)$  chiral unitary approach based on the ChPT [3, 4, 5]. Precision measurements on  $\eta$  and  $\eta'$  would be very helpful, and provide useful information in our understanding of low energy QCD. Especially, the  $\eta \rightarrow 3\pi$  process is very interesting to verify the description of isospin violation in ChPT. The situation has never been clear on this mechanism. A precise analysis on the corresponding Dalitz plot parameters would be very helpful.

The rare decays of  $\eta$  and  $\eta'$  mesons also serve as a test of the Standard Model (SM) at low energy. In this paper, we are trying to give a review of  $\eta$  and  $\eta'$  physics at BES-III by using the decay of  $\psi$ .

## THE PRODUCTION OF $\eta$ AND $\eta'$ AT BES-III

Beginning in mid-2008, the BEPC-II/BES-III was operated at center-of-mass (CM) energies corresponding to  $\sqrt{s} = 2.0 - 4.6$  GeV. The design luminosity over this energy region ranges from  $1 \times 10^{33} \text{cm}^{-2} \text{s}^{-1}$  down to about  $0.6 \times 10^{33} \text{cm}^{-2} \text{s}^{-1}$  [6], yielding around  $5 \text{ fb}^{-1}$  each year at  $\psi(3770)$  above  $D_s^+ D_s^-$  threshold and  $3 \text{ fb}^{-1}$  at  $J/\psi$  peak in one year's running with full luminosity [6]. These integrated luminosities correspond to samples of 2.0 million  $D_s^+ D_s^-$ , 30 million  $D\bar{D}$  pairs and  $10 \times 10^9$   $J/\psi$  decays. Table I summarizes the data set per year at BES-III [7]. In this paper, the sensitivity studies are based on  $3 \text{ fb}^{-1}$  luminosity at the  $J/\psi$  or  $\psi(2S)$  peak for  $\eta$  and  $\eta'$  physics.

In tables II and III, the dominant decay channels of  $J/\psi$  or  $\psi(2S)$  decaying into final states involving  $\eta$  or  $\eta'$  mesons are listed. With one year's luminosity at  $J/\psi$  ( $\psi(2S)$ ) peak, we expect to obtain about 63 million  $\eta$  decays and 61 million  $\eta'$  decays, respectively. At BEPC-II, the background is small and the event topology is simple comparing to the other experiments. The decays of  $\eta$  and  $\eta'$  can be studied with these clean samples, especially, it

TABLE I:  $\tau$ -Charm productions at BEPC-II in one year's running ( $10^7 s$ ).

Data Sample	Central-of-Mass (MeV)	#Events per year
$J/\psi$	3097	$10 \times 10^9$
$\tau^+\tau^-$	3670	$12 \times 10^6$
$\psi(2S)$	3686	$3.0 \times 10^9$
$D^0\bar{D}^0$	3770	$18 \times 10^6$
$D^+D^-$	3770	$14 \times 10^6$
$D_s^+D_s^-$	4030	$1.0 \times 10^6$
$D_s^+D_s^-$	4170	$2.0 \times 10^6$

will be one of the best place to study  $\eta'$  physics.

TABLE II: The production of  $\eta$  meson at BES-III in charmonium decays by assuming  $10 \times 10^9$   $J/\psi$  and  $3.0 \times 10^9$   $\psi(2S)$  events can be collected per year.

Decay mode	Combined branching fraction ( $\times 10^{-4}$ )	#Events per year
$J/\psi \rightarrow \gamma\eta$	$(9.8 \pm 1.0)$	$9.8 \times 10^6$
$J/\psi \rightarrow \phi\eta(\phi \rightarrow K^+K^-)$	$(3.69 \pm 0.39)$	$3.69 \times 10^6$
$J/\psi \rightarrow \omega\eta(\omega \rightarrow \pi^+\pi^-\pi^0)$	$(15.5 \pm 1.8)$	$15.5 \times 10^6$
$J/\psi \rightarrow \rho\eta(\rho \rightarrow \pi^+\pi^-)$	$(1.93 \pm 0.23)$	$1.93 \times 10^6$
$J/\psi \rightarrow p\bar{p}\eta$	$(20.9 \pm 1.8)$	$20.9 \times 10^6$
$\psi(2S) \rightarrow \eta J/\psi(J/\psi \rightarrow l^+l^-)$	$(37.5 \pm 0.8)$	$11.25 \times 10^6$
Total		$63.1 \times 10^6$

## HADRONIC DECAYS OF $\eta$ AND $\eta'$

Hadronic decays of  $\eta$ ,  $\eta' \rightarrow \pi^+\pi^-\pi^0$  and  $\pi^0\pi^0\pi^0$  can be utilized to extract  $m_d - m_u$ . The  $3\pi$ -decay of  $\eta$  or  $\eta'$  violates iso-spin invariance. In case of the  $\pi^0\pi^0\pi^0$  system the two pions can have  $I_{2\pi} = 0, 1, 2$  but coupling with the remaining pion to  $I_{3\pi} = 0$  is only possible if  $I_{2\pi} = 1$ . However, the  $(\pi^0\pi^0)_{I=1}$  dose not exist due to requirement of Bose-Einstein statistics

TABLE III: The production of  $\eta'$  meson at BES-III in charmonium decays by assuming  $10 \times 10^9$   $J/\psi$  and  $3.0 \times 10^9$   $\psi(2S)$  events can be collected per year.

Decay mode	Combined branching fraction ( $\times 10^{-4}$ )	#Events per year
$J/\psi \rightarrow \gamma\eta'$	$(47.1 \pm 2.7)$	$47.1 \times 10^6$
$J/\psi \rightarrow \phi\eta'(\phi \rightarrow K^+K^-)$	$(1.97 \pm 0.34)$	$1.97 \times 10^6$
$J/\psi \rightarrow \omega\eta'(\omega \rightarrow \pi^+\pi^-\pi^0)$	$(1.62 \pm 0.19)$	$1.62 \times 10^6$
$J/\psi \rightarrow \rho\eta'(\rho \rightarrow \pi^+\pi^-)$	$(1.05 \pm 0.18)$	$1.05 \times 10^6$
$J/\psi \rightarrow p\bar{p}\eta'$	$(9.0 \pm 4.0)$	$9.0 \times 10^6$
Total		$60.74 \times 10^6$

and as a consequence the decay  $\eta(\eta') \rightarrow \pi^0\pi^0\pi^0$  has to violate isospin. In the case of the  $\eta(\eta') \rightarrow \pi^+\pi^-\pi^0$  decay one can write [10]

$$(3\pi)_{I=0} = \sqrt{\frac{1}{3}}[(\pi^+\pi^0)_{I=1}|\pi^-\rangle - (\pi^+\pi^-)_{I=1}|\pi^0\rangle + (\pi^-\pi^0)_{I=1}|\pi^+\rangle], \quad (1)$$

where  $(\pi^+\pi^0)_{I=1} = \sqrt{\frac{1}{2}}[|\pi^+\rangle|\pi^0\rangle - |\pi^0\rangle|\pi^+\rangle]$ ,  $(\pi^+\pi^-)_{I=1} = \sqrt{\frac{1}{2}}[|\pi^+\rangle|\pi^-\rangle - |\pi^-\rangle|\pi^+\rangle]$ , and  $(\pi^-\pi^0)_{I=1} = \sqrt{\frac{1}{2}}[-|\pi^-\rangle|\pi^0\rangle + |\pi^0\rangle|\pi^-\rangle]$ , one can obtain the full wave function for the  $3\pi$  system as :

$$(3\pi)_{I=0} = \sqrt{\frac{1}{6}}[|\pi^+\rangle|\pi^0\rangle|\pi^-\rangle - |\pi^0\rangle|\pi^+\rangle|\pi^-\rangle - |\pi^+\rangle|\pi^-\rangle|\pi^0\rangle + |\pi^-\rangle|\pi^+\rangle|\pi^0\rangle - |\pi^-\rangle|\pi^0\rangle|\pi^+\rangle + |\pi^0\rangle|\pi^-\rangle|\pi^+\rangle], \quad (2)$$

which is always antisymmetric against any exchange of pions. In particular, we have  $C(3\pi)_{I=0} = -(3\pi)_{I=0}$ . While it is  $C = +1$  for  $\eta(\eta')$ . Therefore the decay  $\eta(\eta') \rightarrow \pi^+\pi^-\pi^0$  violates  $C$  or  $I$ . On the other hand there exist a  $G$  operator which is constructed from the  $C$  parity and isospin  $I_2$  operators as  $G = Ce^{i\pi I_2}$ , and the decay  $\eta(\eta') \rightarrow \pi^+\pi^-\pi^0$  should also violate the  $G$  parity.

According to Sutherland's theorem, electromagnetic contributions to the process are very small [11] and the decay is induced dominantly by the strong interaction via the  $u$ ,  $d$  mass difference. Based on the following two assumptions: (1) the decay  $\eta' \rightarrow \pi^0\pi^+\pi^-$  proceeds entirely via  $\eta' \rightarrow \eta\pi^+\pi^-$  followed by  $\pi^0-\eta$  mixing; (2) both decay amplitudes are "essentially

*constant*” over phase space on the Dalitz plot, Gross, Treiman and Wilczek claimed that [12]

$$r = \frac{\Gamma(\eta' \rightarrow \pi^0 \pi^+ \pi^-)}{\Gamma(\eta' \rightarrow \eta \pi^+ \pi^-)} = (16.8) \frac{3}{16} \left( \frac{m_d - m_u}{m_s} \right)^2, \quad (3)$$

However recently Borasoy *et al.* claimed that the light quark masses cannot be extracted from the ratio [13, 14] since the results from the full chiral unitary approach are in plain disagreement with these two assumptions. It turns out that more precise experimental data on  $\eta$  and  $\eta'$  decays are needed. An improvement of the experimental situation is foreseen in the near future due to the upcoming data from WASA-at-COSY [15], MAMI-C [16] and KLOE [17]. Here, we would address the clean data samples from  $\psi$  decays at BES-III [6].

TABLE IV: The production of  $\eta(\eta') \rightarrow 3\pi$  decay at BES-III in charmonium decays by assuming  $10 \times 10^9$   $J/\psi$  and  $3.0 \times 10^9$   $\psi(2S)$  events can be collected per year.

Decay mode	Branching fraction (%)	#Events per year
$\eta \rightarrow \pi^0 \pi^+ \pi^-$	$(22.73 \pm 0.28)$	$14.3 \times 10^6$
$\eta \rightarrow \pi^0 \pi^0 \pi^0$	$(32.56 \pm 0.23)$	$20.5 \times 10^6$
$\eta' \rightarrow \eta \pi^+ \pi^-$	$(44.6 \pm 1.4)$	$27.2 \times 10^6$
$\eta' \rightarrow \eta \pi^0 \pi^0$	$(20.7 \pm 1.2)$	$12.6 \times 10^6$
$\eta' \rightarrow \pi^0 \pi^+ \pi^-$	$(0.37^{+0.11}_{-0.09} \pm 0.04)$ [9]	$0.23 \times 10^6$
$\eta' \rightarrow \pi^0 \pi^0 \pi^0$	$(0.154 \pm 0.026)$	$0.09 \times 10^6$

The  $\eta/\eta' \rightarrow 3\pi$  is an ideal laboratory for testing ChPT. From a fit to the Dalitz plot density distribution one can make precise determinations of the parameters that characterize the decay amplitude or. One can choose two of the pion energies ( $T_+, T_-, T_0$ ) in the  $\eta$  rest frame, two of the three combinations of the two-pion masses squared ( $m_{+-}^2, m_{-0}^2, m_{0+}^2$ ) also called ( $s, t, u$ ). The Dalitz plot distribution for the charged decay channel is described by the following two variables:

$$\begin{aligned} X &= \sqrt{3} \frac{T_+ - T_-}{Q_c} = \frac{\sqrt{3}(u - t)}{2m_\eta Q_c}, \\ Y &= \frac{3T_0}{Q_c} - 1 = \frac{3[(m_\eta - m_{\pi^0})^2 - s]}{2m_\eta Q_c} - 1, \end{aligned} \quad (4)$$

where  $Q_c = T_0 + T_+ + T_- = m_\eta - 2m_\pi - m_{\pi^0}$ . For the neutral decay channel it is convenient

to use one fully symmetrized coordinate:

$$Z = \frac{2}{3} \sum_{i=1}^3 \left( \frac{3T_i}{Q_n} - 1 \right)^2 = X^2 + Y^2, \quad (5)$$

with  $Q_n = m_\eta - 3m_{\pi^0}$ , in order to reflect symmetry in all Mandelstam variables.

The squared absolute values of the two decay amplitudes are expanded around the center of the corresponding Dalitz plot for  $\eta/\eta' \rightarrow \pi^0\pi^+\pi^-$  in order to obtain the Dalitz slope parameters [18] :

$$|A_c(X, Y)|^2 = |\mathcal{N}_c|^2 [1 + aY + bY^2 + cX + dX^2 + eXY + \dots], \quad (6)$$

while for the decays into three identical particles Bose symmetry dictates the form

$$|A_n(X, Y)|^2 = |\mathcal{N}_n|^2 [1 + 2\alpha Z + \dots], \quad (7)$$

For the charged channel odd terms in  $X$  are forbidden due to charge conjugation symmetry. The parameters ( $a, b, c, d, e$  and  $\alpha$ ) can be obtained from fits to the observed Dalitz plot density, and can be computed by the theory.

In table IV, we estimate the produced number of events for various hadronic  $\eta$  and  $\eta'$  decay at BES-III with one year's data taking. There are about 14 million  $\eta \rightarrow \pi^0\pi^+\pi^-$  and 0.23 million  $\eta' \rightarrow \pi^0\pi^+\pi^-$  events produced each year, respectively. By considering the detector coverage and reconstruction efficiencies for charged and neutral tracks at BES-III, the selection efficiency for  $\eta/\eta' \rightarrow \pi^0\pi^+\pi^-$  mode is estimated to be 30% [6], and is constant over the Dalitz plots. Thus the expected observed number of events in the Dalitz plot is about  $N_{exp} = 4.2$  million for  $\eta \rightarrow \pi^0\pi^+\pi^-$  decay or  $N_{exp} = 0.07$  million for  $\eta' \rightarrow \pi^0\pi^+\pi^-$  decay. At KLOE, about 6.6 million of  $\eta \rightarrow \pi^0\pi^+\pi^-$  decays should be selected after considering the selection efficiency in  $2.5 \text{ fb}^{-1}$  data [17]. We expect that the Dalitz parameter can be measured almost at the same level of sensitivity for the  $\eta$  decay at BES-III.

Some specific integrated asymmetries as defined in reference [19] are very sensitive in assessing the possible contributions to  $C$ -violation in amplitudes with fixed  $\Delta I$ . In particular left-right asymmetry tests  $C$ -violation with no specific  $\Delta I$  constraint. One can calculate the asymmetry as

$$A_{LR} = \frac{N_+ - N_-}{N_+ + N_-}, \quad (8)$$

where  $N_+$  is the number of events for which  $\pi^+$  has greater energy than  $\pi^-$ , and  $N_-$  is the number of events for which the  $\pi^-$  has the greater energy in the  $\eta$  rest system. One

can also measure the quadrant asymmetry  $A_Q$  and sextant asymmetry  $A_S$  as defined in reference [19]. The quadrant asymmetry is sensitive to an  $I = 2$  final state, while the sextant asymmetry is sensitive to an  $I = 0$   $C$ -invariance-violating final state [20, 21]. With 4.2 million  $\eta \rightarrow \pi^0 \pi^+ \pi^-$  events at BES-III, the sensitivity of these asymmetry could be  $7.0 \times 10^{-4}$ , which is one order lower than the current PDG measurements [8]

For the neutral channel  $\eta/\eta' \rightarrow \pi^0 \pi^0 \pi^0$  decay, assuming that the averaged selection efficiency is 20%, we should expect that about 4.1 million of  $\eta \rightarrow 3\pi^0$  and 0.02 million  $\eta' \rightarrow 3\pi^0$  decays can be selected in the Dalitz plots at BES-III. With these high statistics and low background samples, one can make more precise measurement of the slope parameter  $\alpha$  as shown in formula 7. The best measurement of  $\alpha$  is  $\alpha = -0.032 \pm 0.003$  which is from the Crystal Ball at MAMI-C [22] by using about 3 million  $\eta$  decay events. The result is within errors compatible with the result from KLEO,  $\alpha = -0.027 \pm 0.004(stat)_{-0.006}^{+0.004}(syst)$ , based on 650 thousand events [23]. We expect more precision measurement will be obtained at BES-III with 4.1 million of  $\eta \rightarrow 3\pi^0$  events.

For the  $\eta' \rightarrow \eta \pi^+ \pi^-$  and  $\eta' \rightarrow \eta \pi^0 \pi^0$  decays, about 27 million and 12 million decay events could be detected at BES-III each year, respectively. Since the mass of  $\eta'$  meson is large enough, in this case, the contributions of  $\sigma$ ,  $a_0$  and  $f_0(980)$  resonances and their interference on the Dalitz plots dominate [24]. It will be very interesting to study the  $\eta\pi$  and  $\pi\pi$  scattering in these decay modes at BES-III with the huge data set.

## RARE DECAYS OF $\eta$ AND $\eta'$

Decays of  $\eta$  and  $\eta'$  mesons into a lepton-antilepton pairs,  $\eta/\eta' \rightarrow l^+ l^-$ , represent a potentially important channel to look for effects of new physics [25]. The dominant mechanism within the SM is a second order electromagnetic process, additionally suppressed by helicity conservation, involving two virtual photons  $\eta \rightarrow \gamma^* \gamma^*$ , which is sensitive to the form factor  $F_{\eta\gamma^*\gamma^*}$  of the transition  $\eta \rightarrow \gamma^* \gamma^*$  with off-shell photons [26]. The imaginary part of the decay amplitude can be uniquely related to the decays width of the  $\eta \rightarrow \gamma\gamma$  decay. The experimental value of the  $\Gamma(\eta \rightarrow \gamma\gamma)$  leads to a lower limit (the unitarity bound) of the branching ratio:  $BR(\eta \rightarrow e^+ e^-) \geq 1.7 \times 10^{-9}$  and  $BR(\eta \rightarrow \mu^+ \mu^-) \geq 4.4 \times 10^{-6}$  when the real part of the decay amplitude is neglected [25, 27]. The measured branching fraction,  $BR(\eta \rightarrow \mu^+ \mu^-) = (5.7 \pm 0.8) \times 10^{-6}$  [8], is consistent with this limit.

The real part of the amplitude of the  $\eta \rightarrow e^+e^-$  decay can be estimated using the measured value of  $BR(\eta \rightarrow \mu^+\mu^-)$  [28, 29, 30, 31]. The assumption that the ratio between Im and Re parts of the amplitudes for the  $\eta \rightarrow e^+e^-$  and  $\eta \rightarrow \mu^+\mu^-$  is the same leads to the prediction  $BR(\eta \rightarrow e^+e^-) \simeq 6 \times 10^{-9}$ . The limit for  $\eta \rightarrow e^+e^-$  is much lower than for other decays of  $\pi^0$  and  $\eta$  into lepton-antilepton pairs. This makes the  $\eta \rightarrow e^+e^-$  decay rate sensitive to a possible exotic contribution. The best experimental upper limit for the  $BR(\eta \rightarrow e^+e^-)$  comes from the CLEO-II as listed in table V. By the way, the decays  $\pi^0 \rightarrow e^+e^-$ ,  $\eta \rightarrow \mu^+\mu^-$  and  $e^+e^-$  are also important in order to estimate long range contribution to the decay  $K_L \rightarrow \mu^+\mu^-$  [29].

Recently, the KTeV experiment at Fermilab has made the first observation of the decay  $\pi^0 \rightarrow e^+e^-$  to be [32]:

$$BR(\pi^0 \rightarrow e^+e^-) = (7.49 \pm 0.29 \pm 0.25) \times 10^{-8}, \quad (9)$$

which is 3 standard deviations higher than the theoretical prediction [33, 34, 35]. It is interesting to search for the other neutral pseudoscalar meson decays into lepton pairs and to compare with theoretical predictions. These probes will offer a way to study long-distance dynamics in the Standard Model. At BESIII, leptonic decays  $\eta/\eta' \rightarrow e^+e^-$ ,  $\mu^+\mu^-$ ,  $e^+e^-e^+e^-$ ,  $\mu^+\mu^-\mu^+\mu^-$  and  $e^+e^-\mu^+\mu^-$  can be measured with sensitivities at  $10^{-7}$  as listed in table V and VI. Most of the limits will be improved by one or two orders by using data with one year luminosity in  $J/\psi$  and  $\psi(2S)$  decays. We will also test C-invariance by improving the upper limits on the C-forbidden decays  $\eta/\eta' \rightarrow \pi^0e^+e^-$ ,  $\pi^0\mu^+\mu^-$ ,  $3\gamma$  and  $\eta' \rightarrow \eta e^+e^-$ ,  $\eta\mu^+\mu^-$ . We will test CP-invariance by searching for  $\eta/\eta' \rightarrow \pi\pi$  and  $4\pi^0$  decays [36]. The first experimental run at  $J/\psi$  and  $\psi(2S)$  peaks has been conducted at BES-III/BEPC-II. We expect to obtain more data so that the sensitivities listed in table V and VI. can be reached.

The  $\eta(\eta') \rightarrow \pi^+\pi^-e^+e^-$  decay is interesting as test of  $CP$  violation which is motivated by corresponding test in  $K_L$  decays. A recent prediction and observations of an asymmetry were made in the distribution of angles between the  $\pi^+\pi^-$  and  $e^+e^-$  production planes in  $K_L \rightarrow \pi^+\pi^-e^+e^-$  decay [37]. These observations have triggered theoretical speculations that a similar observation in  $\eta \rightarrow \pi^+\pi^-e^+e^-$  decay might reveal unexpected mechanisms of  $CP$  violation in flavor conserving processes [38, 39]. At BES-III, we can observe a  $CP$ -violating



TABLE V: The sensitivity of  $\eta$  rare and forbidden decays at BES-III. The expected sensitivities are estimated by considering the detector efficiencies for different decay mode at BES-III. We assume no background dilution and the observed number of signal events is zero. The BES-III limit refers to a 90% confidence level.

Decay mode	Best upper limits	BES-III limit
	90% CL	with one year's luminosity
$\eta \rightarrow e^+e^-$	$7.7 \times 10^{-5}$	$0.7 \times 10^{-7}$
$\eta \rightarrow \mu^+\mu^-$	$(5.8 \pm 0.8) \times 10^{-6}$	$0.8 \times 10^{-7}$
$\eta \rightarrow e^+e^-e^+e^-$	$6.9 \times 10^{-5}$	$0.9 \times 10^{-7}$
$\eta \rightarrow \mu^+\mu^-\mu^+\mu^-$	—	$1.5 \times 10^{-7}$
$\eta \rightarrow \pi^+\pi^-e^+e^-$	$(4.2 \pm 1.2) \times 10^{-4}$	$1.3 \times 10^{-7}$
$\eta \rightarrow \pi^+\pi^-\mu^+\mu^-$	—	$1.4 \times 10^{-7}$
$\eta \rightarrow \pi^0\mu^+\mu^-$	$5 \times 10^{-6}$	$1.5 \times 10^{-7}$
$\eta \rightarrow \pi^0e^+e^-$	$4 \times 10^{-5}$	$1.3 \times 10^{-7}$
$\eta \rightarrow \pi^0\gamma$	$9 \times 10^{-5}$	$1.2 \times 10^{-7}$
$\eta \rightarrow \pi^0\pi^0$	$3.5 \times 10^{-4}$	$1.8 \times 10^{-7}$
$\eta \rightarrow \pi^+\pi^-$	$1.3 \times 10^{-5}$	$0.8 \times 10^{-7}$
$\eta \rightarrow \mu^+e^- + \mu^-e^+$	$6 \times 10^{-6}$	$0.8 \times 10^{-7}$
$\eta \rightarrow \text{invisible}$	$6 \times 10^{-4}$	$60 \times 10^{-7}$

asymmetry in the  $CP$  and  $T$ -odd variable  $\sin\phi\cos\phi$ ,

$$A = \frac{N_{\sin\phi\cos\phi>0.0} - N_{\sin\phi\cos\phi<0.0}}{N_{\sin\phi\cos\phi>0.0} + N_{\sin\phi\cos\phi<0.0}}, \quad (10)$$

where  $\phi$  is the angle between the  $e^+e^-$  and  $\pi^+\pi^-$  planes in the  $\eta$  center of mass system. This asymmetry implies, with the mild assumption of unitarity to avoid exotic  $CPT$  violation [38], time reversal symmetry violation. The quantity  $\sin\phi\cos\phi$  is given by  $(\hat{n}_{ee} \times \hat{n}_{\pi\pi}) \cdot \hat{z}(\hat{n}_{ee} \cdot \hat{n}_{\pi\pi})$ , where the  $\hat{n}$ 's are the unit normals and  $\hat{z}$  is the unit vector in the direction of the  $\pi\pi$  in the  $\eta$  center of mass system. The measured branching fraction is  $BR(\eta \rightarrow \pi^+\pi^-e^+e^-) = (4.2 \pm 1.2) \times 10^{-4}$  [8]. About 26 thousand events are expected to be produced at BES-III. Assuming that the efficiency is about 30%, we expect that the sensitivity to measure the  $CP$  asymmetry is about 1%. A measurement done with a sensitivity better than  $10^{-2}$  for the

TABLE VI: The sensitivity of  $\eta'$  rare and forbidden decays at BES-III. The expected sensitivities are estimated by considering the detector efficiencies for different decay mode at BES-III. We assume no background dilution and the observed number of signal events is zero. The BES-III limit refers to a 90% confidence level.

Decay mode	Best upper limits	BES-III limit
	90% CL	with one year's luminosity
$\eta' \rightarrow e^+e^-$	$2.1 \times 10^{-7}$	$0.7 \times 10^{-7}$
$\eta' \rightarrow \mu^+\mu^-$	—	$0.8 \times 10^{-7}$
$\eta' \rightarrow e^+e^-e^+e^-$	—	$0.9 \times 10^{-7}$
$\eta' \rightarrow \mu^+\mu^-\mu^+\mu^-$	—	$1.6 \times 10^{-7}$
$\eta' \rightarrow \pi^+\pi^-e^+e^-$ [9]	$(25_{-9}^{+12} \pm 5) \times 10^{-4}$	$1.4 \times 10^{-7}$
$\eta' \rightarrow \pi^+\pi^-\mu^+\mu^-$ [9]	$2.4 \times 10^{-4}$	$1.5 \times 10^{-7}$
$\eta' \rightarrow \pi^0\mu^+\mu^-$	$6.0 \times 10^{-5}$	$1.6 \times 10^{-7}$
$\eta' \rightarrow \pi^0e^+e^-$	$1.4 \times 10^{-3}$	$1.3 \times 10^{-7}$
$\eta' \rightarrow \pi^0\gamma$	—	$1.2 \times 10^{-7}$
$\eta' \rightarrow \pi^0\pi^0$	$9.0 \times 10^{-4}$	$1.9 \times 10^{-7}$
$\eta' \rightarrow \pi^+\pi^-$	$2.9 \times 10^{-3}$	$0.8 \times 10^{-7}$
$\eta' \rightarrow \mu^+e^- + \mu^-e^+$	$4.7 \times 10^{-4}$	$0.8 \times 10^{-7}$
$\eta' \rightarrow \text{invisible}$	$9.5 \times 10^{-4}$ [9]	$140 \times 10^{-7}$
$\eta' \rightarrow \eta e^+e^-$	$2.4 \times 10^{-3}$	$2.4 \times 10^{-7}$
$\eta' \rightarrow \eta\mu^+\mu^-$	$1.5 \times 10^{-5}$	$3.1 \times 10^{-7}$

asymmetry will provide a stringent constraint for new physics proposed by D. N. Gao [39].

Invisible decays of  $\eta$  and  $\eta'$  mesons offer a window into what may lie beyond the Standard Model [41, 42]. The reason is that apart from neutrinos, the Standard Model includes no other invisible final particles that these states can decay into. It is such a window that we intend to further explore by presenting here the first experimental limits on invisible decays of the  $\eta$  and  $\eta'$ , which complement the limit of  $2.7 \times 10^{-7}$  recently established in [43] for the invisible decays of the  $\pi^0$ .

Theories beyond the Standard Model generally include new physics, such as, possibly, light dark matter (LDM) particles [44]. These can have the right relic abundance to consti-

tute the nonbaryonic dark matter of the Universe, if they are coupled to the SM through a new light gauge boson  $U$  [45], or exchanges of heavy fermions. It is also possible to consider a light neutralino with coupling to the Standard Model mediated by a light scalar singlet in the next-to-minimal supersymmetric standard model [46].

The BES-II Collaboration searched for the invisible decay modes of  $\eta$  and  $\eta'$  for the first time in  $J/\psi \rightarrow \phi\eta(\eta')$  using the 58 million  $J/\psi$  events at BES II [47]. They obtained limits on the ratio,  $\frac{\mathcal{B}(\eta(\eta') \rightarrow \text{invisible})}{\mathcal{B}(\eta(\eta') \rightarrow \gamma\gamma)}$ . The upper limits at the 90% confidence level are  $1.65 \times 10^{-3}$  and  $6.69 \times 10^{-2}$  for  $\frac{\mathcal{B}(\eta \rightarrow \text{invisible})}{\mathcal{B}(\eta \rightarrow \gamma\gamma)}$  and  $\frac{\mathcal{B}(\eta' \rightarrow \text{invisible})}{\mathcal{B}(\eta' \rightarrow \gamma\gamma)}$ , respectively, corresponding to upper limits on the rates for  $\eta \rightarrow \text{invisible}$  of  $6.0 \times 10^{-4}$  and for  $\eta' \rightarrow \text{invisible}$  of  $1.4 \times 10^{-3}$ . CLEO-c has almost two times better limit than that from BES-II for  $\eta' \rightarrow \text{invisible}$  decay as shown in table VI [9]. At BES-III, the sensitivity of the invisible decays will be improved by two orders of magnitude with high statistics data as listed in table V and VI.

## SUMMARY

A mini-review of  $\eta$  and  $\eta'$  physics at BES-III has been done. With one year's luminosity data, about 63 million  $\eta$  decays and 61 million  $\eta'$  decays can be collected at BES-III. The hadronic decays of  $\eta$  and  $\eta'$  can be studied, especially parameters for the Dalitz decays of  $\eta$  could be extracted from about 4.2 million  $\eta$  events, so that the prediction of ChPT will be tested. The rare and forbidden decays of  $\eta$  and  $\eta'$  could be reached at BES-III, and the sensitivity of these decay is at the level of  $10^{-7}$ . New physics beyond the standard Model can be probed at low energy. At BES-III,  $\eta$  and  $\eta'$  decay samples are clean, and the event topology is simple so that events can be easily reconstructed. More fruit results will be seen from BES-III experiment.

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